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## 10 — Abstract —

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11 This document describes MAEDM-OCM, a first generation memetic algorithm for the one-sided  
12 crossing minimization problem (OCM), which was submitted to the heuristic track of the Parameterized Algorithms and Computational Experiments Challenge 2024. In this variant of OCM, given  
13 a bipartite graph with vertices  $V = A \cup B$ , only the nodes of the layer  $B$  can be moved. The  
14 main features of MAEDM-OCM are the following: the diversity is managed explicitly through the  
15 Best-Non-Penalized (BNP) survivor strategy, the intensification is based on Iterated Local Search  
16 (ILS), and the cycle crossover is applied. Regarding the intensification step, the neighborhood is  
17 based on shifts and only a subset of the neighbors in the local search are explored. The use of  
18 the BNP replacement was key to attain a robust optimizer. It was also important to incorporate  
19 low-level optimizations to efficiently calculate the number of crossings and to reduce the requirements  
20 of memory. In the case of the longest instances ( $|B| > 17000$ ) the memetic approach is not applicable  
21 with the time constraints established in the challenge. In such cases, ILS is applied. The optimizer  
22 is not always applied to the original graph. In particular, twin nodes in  $B$  are grouped in a single  
23 node.  
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28 **Supplementary Material** The source code is freely available at [https://github.com/carlossegurag/](https://github.com/carlossegurag/PaceChallenge24)  
29 [PaceChallenge24](https://github.com/carlossegurag/PaceChallenge24) and <https://zenodo.org/doi/10.5281/zenodo.12512615>

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## 32 **1 Preliminaries**

33 The One-sided Crossing Minimization problem (OCM) involves arranging the nodes of a  
34 bipartite graph in two layers, so that the crossing of edges is minimized when a straight-line  
35 drawing is performed. In the Parameterized Algorithms and Computational Experiments  
36 (PACE) Challenge, the vertices associated to each of the layers ( $A$  and  $B$ ) as well as the  
37 order of the vertices in  $A$  are given. Thus, the problem seeks an order of  $B$  so as to minimize  
38 the number of crossings. Since any order of the nodes in  $B$  is valid, a natural encoding is a  
39 permutation of the vertices in  $B$ , which has been the encoding selected for our method.

40 Regarding the solving strategies, Memetic Algorithms (MAs) are one of the most effective  
41 solvers for NP-hard problems. In fact, in several problems where solutions are encoded as  
42 permutations, MAs are the leading methods. This is the case of the Job-Shop Scheduling  
43 Problem [1] and the Linear Ordering Problem [3], among others. In these cases, the explicit  
44 management of diversity was key to develop robust methods that are able to reach high-

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**Algorithm 1** Memetic Algorithm with Explicit Diversity Management for OCM
 

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**Require:**  $InitFactor$ ,  $N$ (size of population), *Stopping criterion Phase 1 (time1)*, *Global Stopping criterion (time2)*

- 1: **Initialization:** Generate an initial population  $P_0$  with  $N$  individuals. Assign  $i = 0$ .
  - 2: **Iterated Local Search:** Apply Iterated Local Search to every individual in  $P_0$ .
  - 3: **Diversity Initialization:** Calculate the initial desired minimum distance ( $D_0$ ) as the mean distance among individuals in  $P_0$  multiplied by  $InitFactor$ .
  - 4: **while** the execution time of Phase 1 (time1) has not been reached **do**
  - 5:   **Mating Selection:** Perform binary tournament selection on  $P_i$  in order to fill the mating pool with  $N$  parents.
  - 6:   **Variation:** Apply the cycle-based crossover (CX) in the mating pool to create the set  $O_i$  with  $N$  offspring.
  - 7:   **Iterated Local Search:** Apply Iterated Local Search to every individual in  $O_i$ .
  - 8:   **Survivor Selection:** Apply Best-Non Penalized survivor selection strategy (BNP) to create  $P_{i+1}$  by considering  $P_i$  and  $O_i$  as input.
  - 9:    $i = i + 1$
  - 10: **end while**
  - 11: **Iterated Local Search:** Apply Iterated Local Search to the best evaluated permutation so far, until time2 is exhausted
  - 12: **Return** best evaluated permutation.
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45 quality solutions with a high probability. Thus, our team decided to adapt some of the  
 46 principles that were successful in those problems to the OCM.

47 **2 MAEDM-OCM: a first generation memetic algorithm for the**  
 48 **one-sided crossing minimization problem**

49 The Memetic Algorithm with Explicit Diversity Management for the One-sided Crossing  
 50 Minimization problem (MAEDM-OCM) is a first-generation MA. MAEDM-OCM applies a  
 51 set of operators that have already proven to be effective for permutation encoding. Given that  
 52 short-term executions are performed, a first-generation MA is applied. Thus, a population-  
 53 based approach is combined with a non-adaptive intensification scheme which in this case is  
 54 Iterated Local Search (ILS). Algorithm 1 shows the general working operation of our proposal.  
 55 Differently to most MAs, the method is divided in two phases. In the first phase (lines  
 56 1-10) a traditional MA is considered. In the second phase (line 11), ILS is applied to the  
 57 best solution found so far. The reason to incorporate this second phase is that for medium  
 58 and large instances, the stopping criterion used in the challenge is not enough to evolve a  
 59 large number of generations. Thus, there might be opportunity for further improvements by  
 60 applying ILS. In spite of this additional change, the most important decisions that affect the  
 61 performance of MAEDM-OCM are related to the specific components that were used in the  
 62 first phase. In the following, the working operation of each component of the first phase is  
 63 described.

64 Our approach starts by initializing a population with  $N$  individuals, where each permu-  
 65 tation is equiprobable (Line 1). Then, each solution is improved with ILS (Line 2). ILS  
 66 uses a first-improvement stochastic hill-climber that considers the shift neighborhood [2].  
 67 This neighborhood is selected because it can be explored efficiently by storing the crossing  
 68 number matrix. Neighbors are generated by moving a vertex in the given permutation to

69 an alternative position and shifting all the vertices in the intermediate positions. However,  
 70 not all the moves are taken into account. Each number is moved to the left and right until  
 71 its worsening is larger than a threshold value or until it reaches the first or last position.  
 72 Then, the best move is accepted. The worsening threshold is equal to the median value  
 73 of the crossing number matrix multiplied by *cuttingMult*, which is a parameter of the  
 74 optimizer. Regarding the perturbations performed by ILS, three different alternatives were  
 75 used equiprobably: swap a set of *SwapSize* pairs of positions, do a random shuffle of a block  
 76 with size *permBlock* or move a block with a size that is selected randomly between 1 and 10  
 77 to a random position of the permutation.

78 An important feature of our approach is that it considers diversity explicitly. This is done  
 79 with the replacement strategy, which works by setting a minimum desired distance that is  
 80 updated during the run. Similarly to [1], the distances that appear in the initial population  
 81 are used to set the initial desired distance ( $D_0$ ) (Line 3). In particular,  $D_0$  is calculated as the  
 82 mean distance among all the individuals in the initial population multiplied by *InitFactor*,  
 83 which is a parameter of MAEDM-OCM. In order to calculate  $D_0$ , the Spearman's footrule  
 84 distance [4] is employed.

85 MAEDM-OCM evolves a set of generations until a given stopping criterion is reached  
 86 (Lines 4-10). At each generation, a set of  $N$  parents is selected using binary tournaments  
 87 (Line 5). Then, the cycle-based crossover is applied (Line 6), and ILS is used to intensify  
 88 (Line 7). Finally, the diversity-aware replacement strategy called BNP is applied (Line 8).  
 89 BNP is an elitist survivor selection strategy that avoids the survival of too close solutions.  
 90 The meaning of too close is defined dynamically. At the initial stages it forces larger distances  
 91 between solutions with the aim of promoting exploration, whereas at the final stages closer  
 92 solutions are accepted with the aim of promoting exploitation. The details are given in [1].

## 93 2.1 Other Improvements and Treatment of Large Instances

94 There were several low-level optimizations that were important to the efficiency:

- 95 ■ The performance of the local search was improved by storing the crossing number matrix  
 96 and an improvement matrix that contains the gain of swapping two consecutive nodes of  
 97 a solution.
- 98 ■ The crossing number matrix is calculated efficiently by using data structures such as  
 99 balanced search trees or the two-pointer technique, depending on the size of the instance.
- 100 ■ The data types for storing the matrices is adapted depending on the requirements of the  
 101 instance.
- 102 ■ Twin vertices in  $B$  are grouped for creating a shorter graph with parallel edges that can  
 103 be used to solve the original problem with a reduced search space.

104 In spite of the efforts for efficiency, the stopping time established for the challenge was not  
 105 large-enough for using the two phases of MAEDM-OCM in the longest instances. In instances  
 106 with  $|B| > 17000$ , only the second phase is used, i.e. it directly applies ILS. Moreover, in this  
 107 case the solution is not created randomly. Instead, for each edge  $(a_i, b_i)$  an score is assigned  
 108 which is equal to the amount of existing edges with its  $A$ -endpoint lower than  $a_i$  and its  
 109  $B$ -endpoint different to  $b_i$ . Then, each vertex of  $B$  is assigned an score equal to the mean of  
 110 its adjacent edges. The initial solution greedily sorts the vertices in  $B$  by increasing score.

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